

# Decision making Problems of Membership Matrix and Comparison matrix under Fuzzy Environment

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**Abstract :** Making decisions is undoubtedly one of the most fundamental activities of human beings. We are all faced in our daily life with Varieties of alternative actions available to us and atleast in some instances, we have to decide which of the available actions to take. The field of decision making are the most fruitful and interesting area of application of fuzzy set theory. In real life situations, Uncertain information gathered for decision making requires the use of “fuzzy”. In this paper procedures are presented for medical diagnosis and for fuzzy decision model. Examples are illustrated to verify the proposed approach.

**Keywords :** Medical Diagnosis, Fuzzy Matrix, membership function, Decision Making, Triangular fuzzy Number.

## I. INTRODUCTION

The field of Medicine and decision making are the most fruitful and interesting area of applications of fuzzy set theory. In recent years fuzzy set theory and fuzzy logic are highly suitable and applicable for developing knowledge based system. Making decision is undoubtedly one of the most fundamental activities of human beings. Fuzzy logic has provided to be a powerful tool for decision making systems, such as expert systems and pattern classification systems. Fuzzy set theory has already been used in some medical expert systems. In this paper, we would like to discuss how fuzzy set theory and fuzzy logic can be used for developing knowledge based system in medicine. Some basic definitions of fuzzy set theory has been discussed in section 2. In section 3, a novel approach is presented for medical diagnosis which is also an extension of sanchez’s approach with modified procedure using triangular fuzzy number matrices and its new membership function. In section 4, a procedure is proposed for fuzzy decision model using new relativity function and comparison matrix. In both the sections illustrative example is included to demonstrate the proposed approach. Some conclusions are given in section 5.

## II. PRELIMINARIES

### Definition 2.1 Triangular fuzzy Number

Triangular Fuzzy Number is denoted as  $A = (a_1, a_2, a_3)$ ,  $a_1, a_2, a_3 \in \mathcal{R}$ ,  $a_1 < a_2 < a_3$ .

### Definition 2.2 Triangular fuzzy Number Matrix

Triangular Fuzzy Number Matrix of order  $m \times n$  is defined as  $A = (a_{ij})_{m \times n}$ , where  $a_{ij} = (a_{ijL}, a_{ijM}, a_{ijU})$  is the  $ij$ <sup>th</sup> element of  $A$ .  $a_{ijL}, a_{ijU}$  are the left and right spreads of  $a_{ij}$  respectively and  $a_{ijM}$  is the mean value.

### Definition 2.3 Addition and Subtraction Operation on Triangular fuzzy Number Matrix

Let  $A = (a_{ij})_{n \times n}$  and  $B = (b_{ij})_{n \times n}$  be the two triangular fuzzy number matrices of same order.

#### (i) Addition Operation

$$A + B = (a_{ij} + b_{ij})_{n \times n} \text{ where } a_{ij} + b_{ij} =$$

$(a_{ijL} + b_{ijL}, a_{ijM} + b_{ijM}, a_{ijU} + b_{ijU})$  is the  $ij$ <sup>th</sup> element of  $A + B$ .

#### (ii) Subtration Operation

$A - B = (a_{ij} - b_{ij})_{n \times n}$  where  $a_{ij} - b_{ij} = (a_{ijL} - b_{ijU}, a_{ijM} - b_{ijM}, a_{ijU} - b_{ijL})$  is the  $ij$ <sup>th</sup> element of  $A - B$ . The same condition holds for triangular fuzzy membership number.

### Definition 2.4 Multiplication Operation on Triangular fuzzy Number Matrix

Let  $A = (a_{ij})_{m \times p}$  and  $B = (b_{ij})_{p \times n}$  be the two triangular fuzzy number matrices, then the multiplication operation  $A \cdot B = (c_{ij})_{m \times n}$  where  $c_{ij} = \sum_{k=1}^p a_{ik} b_{kj}$  for  $i = 1, 2, \dots, m$  and  $j = 1, 2, \dots, n$

### Definition 2.5 Max-Min Composition on fuzzy Membership Value

Let  $F_{mn}$  denote the set of all  $m \times n$  matrices over  $F$ . Elements of  $F_{mn}$  are called as fuzzy membership value matrices. For  $A = (a_{ij}) \in F_{mp}$  and  $B = (b_{ij}) \in F_{pn}$ , the max-min product

$$A \circ B = \left( \sup_k \{ \inf \{ a_{ik}, b_{kj} \} \} \right) \in F_{mn}$$

### Definition 2.6 Arithmetic Mean (AM) for triangular fuzzy number :

Let  $A = (a_1, a_2, a_3)$  be a triangular fuzzy number, then  $AM A = \frac{a_1 + a_2 + a_3}{3}$ . The same condition holds for triangular fuzzy membership number.

## III. MEDICAL DIAGNOSIS UNDER FUZZY ENVIRONMENT

Let  $S$  be the set of symptoms of certain diseases,  $D$  is a set of diseases and  $P$  is a set of Patients. The elements of triangular fuzzy number matrix are defined as  $A = (a_{ij})_{m \times l}$  where  $a_{ij} = (a_{ijL}, a_{ijM}, a_{ijU})$  is the  $ij$ <sup>th</sup> element of  $A$ ,  $0 \leq a_{ijL} \leq a_{ijM} \leq a_{ijU} \leq 10$ . Here  $a_{ijL}$  is the lower bound,  $a_{ijM}$  is the moderate value and  $a_{ijU}$  is the upper bound.

**Procedure 3.1**

**Step 1 :** Construct a triangular fuzzy matrix (F,D) over S, where F is a mapping given by  $F: D \rightarrow \check{F}(S)$ ,  $\check{F}(S)$  is a set of all triangular fuzzy sets of S. This matrix is denoted by  $R_0$  which is the fuzzy occurrence matrix or symptom-disease triangular fuzzy number matrix.

**Step 2 :** Construct another triangular fuzzy number matrix ( $F_1, S$ ) over P, where  $F_1$  is a mapping given by  $F_1: S \rightarrow F(P)$ . This matrix is denoted by  $R_s$  which is the patient symptom triangular fuzzy number matrix.

**Step 3 :** Convert the elements of triangular fuzzy number matrix into its membership function as follows : Membership function of  $a_{ij} = (a_{ijL}, a_{ijM}, a_{ijU})$  is defined as

$$\mu_{a_{ij}} = \left( \frac{a_{ijL}}{10} \leq \frac{a_{ijM}}{10} \leq \frac{a_{ijU}}{10} \right), \text{ if } 0 \leq a_{ijL} \leq a_{ijM} \leq a_{ijU} \leq 10, \text{ where } 0 \leq \frac{a_{ijL}}{10} \leq \frac{a_{ijM}}{10} \leq \frac{a_{ijU}}{10} \leq 1.$$

Now, the matrix  $R_0$  and  $R_s$  are converted into triangular fuzzy membership matrices namely  $(R_0)_{mem}$  and  $(R_s)_{mem}$ .

**Step 4 :** Compute the following relation matrices.

$R_1 = (R_s)_{mem}(\cdot)(R_0)_{mem}$  it is calculated using Definition 2.5.

$R_2 = (R_s)_{mem}(\cdot)(J - (R_0)_{mem})$ , where J is the triangular fuzzy membership matrix in which all entries are (1,1,1).  $(J - (R_0)_{mem})$  is the complement of  $(R_0)_{mem}$  and it is called as non symptom-disease triangular fuzzy membership matrix.

$R_3 = (J - (R_s)_{mem})(\cdot)(R_0)_{mem}$ , where  $(J - (R_s)_{mem})$  is the complement of  $R_s$  and it is called as non patient-symptom triangular fuzzy membership matrix.

$R_2$  and  $R_3$  are calculated using subtraction operation and Definition 2.5.

$R_4 = \max\{R_2, R_3\}$ . It is calculated using Definition 2.6

$$R_0 = \begin{matrix} & d_1 & d_2 \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{matrix} (7,7.5,9) \\ (3,3,5.5) \\ (5,6.5,7) \\ (3,4.5,5) \end{matrix} & \begin{matrix} (6,7,8.5) \\ (4.5,6,7) \\ (3.5,5,6.5) \\ (8,9,10) \end{matrix} \end{matrix}$$

**Step 2 :** Again we take  $P = \{p_1, p_2, p_3\}$  as universal set, where  $p_1, p_2$  and  $p_3$  as the universal set, where  $p_1, p_2$  and  $p_3$  represent Patients respectively and  $S = \{s_1, s_2, s_3, s_4\}$  as the set pf parameters.

$$\begin{aligned} \text{Suppose that } F_1(s_1) &= [\langle p_1, (5.5,7,8.5) \rangle, \langle p_2, (3,4.5,5) \rangle, \langle p_3, (6,7.5,8) \rangle] \\ F_1(s_2) &= [\langle p_1, (4,5,6.5) \rangle, \langle p_2, (3.5,6.5,7.5) \rangle, \langle p_3, (3,5,7.5) \rangle] \\ F_1(s_3) &= [\langle p_1, (8,9.5,10) \rangle, \langle p_2, (3,4.5,5) \rangle, \langle p_3, (6.5,7.5,7.5) \rangle] \\ F_1(s_4) &= [\langle p_1, (7.5,8,10) \rangle, \langle p_2, (4,5,6.5) \rangle, \langle p_3, (3,4.5,6) \rangle] \end{aligned}$$

The triangular fuzzy number matrix ( $F_1, S$ ) is another parameterized family of triangular fuzzy matrix and gives a collection of approximate description of patient – Symptoms in the hospital. Thus the triangular fuzzy number matrix ( $F_1, S$ ) represents a relation matrix  $R_s$  called patient-symptom matrix given by

$$R_s = \begin{matrix} & s_1 & s_2 & s_3 & s_4 \\ \begin{matrix} p_1 \\ p_2 \\ p_3 \end{matrix} & \begin{matrix} (5.5,7,8.5) \\ (3,4.5,5) \\ (6,7.5,8) \end{matrix} & \begin{matrix} (4,5,6.5) \\ (3.5,6.5,7.5) \\ (3,5,7.5) \end{matrix} & \begin{matrix} (8,9.5,10) \\ (3,4.5,5) \\ (6.5,7.5,7.5) \end{matrix} & \begin{matrix} (7.5,8,10) \\ (4,5,6.5) \\ (3,4.5,6) \end{matrix} \end{matrix}$$

**Step 3 :**

$$(R_0)_{mem} = \begin{matrix} & d_1 & d_2 \\ \begin{matrix} s_1 \\ s_2 \\ s_3 \\ s_4 \end{matrix} & \begin{matrix} (0.7,0.75,0.9) \\ (0.3,0.3,0.55) \\ (0.5,0.65,0.7) \\ (0.3,0.45,0.5) \end{matrix} & \begin{matrix} (0.6,0.7,0.85) \\ (0.45,0.6,0.7) \\ (0.35,0.5,0.65) \\ (0.8,0.9,1) \end{matrix} \end{matrix}$$

The elements of  $R_1, R_2, R_3, R_4$  is of the form  $Y_{ij} = (y_{ijL}, y_{ijM}, y_{ijU})$  where  $0 \leq y_{ijL} \leq y_{ijM} \leq y_{ijU} \leq 1$ .

$R_5 = R_1 - R_4$ . It is calculated using subtraction operation. The elements of  $R_5$  is of the form  $Z_{ij} = (Z_{ijL}, Z_{ijM}, Z_{ijU}) \in [-1,1]$ , where  $Z_{ijL} \leq Z_{ijM} \leq Z_{ijU}$ .

**Step 5 :** Calculate  $R_6 = AM(Z_{ij})$  and  $Row'_i =$  Maximum of  $i^{th}$  row which helps the decision maker to strongly confirm the disease for the patient.

**Example 3.1**

Suppose there are three patients  $P_1, P_2$  and  $P_3$  in a hospital with symptoms headache, Joint Pains, Vomiting, Diarrhea. Let the Possible diseases relating to the above symptoms be Swine flu and Dengue.

**Step 1 :** We consider the Set  $S = \{s_1, s_2, s_3, s_4\}$  as universal set where  $s_1, s_2, s_3$  and  $s_4$  represent the symptoms headache, Joint Pains, Vomiting, Diarrhea respectively. and the set  $D = \{d_1, d_2\}$ . where  $d_1$  and  $d_2$  represent the parameters Swine flu and Dengue respectively.

Suppose that

$$\begin{aligned} F(d_1) &= [\langle e_1, (7,7.5,9) \rangle, \langle e_2, (3,3.5,5) \rangle, \langle e_3, (5,6.5,7) \rangle, \langle e_4, (3,4.5,5) \rangle] \\ F(d_2) &= [\langle e_1, (6,7,8.5) \rangle, \langle e_2, (4.5,6,7) \rangle, \langle e_3, (3.5,5,6.5) \rangle, \langle e_4, (8,9,10) \rangle] \end{aligned}$$

The triangular fuzzy number matrix ( $F, D$ ) is a parameterized family ( $F(d_1), F(d_2)$ ) of all triangular fuzzy number matrix over the set S and are determined from expert medical documentation. Thus the triangular fuzzy number matrix ( $F, D$ ) represents a relation matrix  $R_0$  and it gives an approximate description of the triangular fuzzy number matrix medical knowledge of the two diseases and their symptoms given by

$$(R_s)_{mem} = \begin{pmatrix} p_1 & \begin{matrix} s_1 \\ (0.55,0.7,0.85) \end{matrix} & \begin{matrix} s_2 \\ (0.4,0.5,0.65) \end{matrix} & \begin{matrix} s_3 \\ (0.8,0.95,1) \end{matrix} & \begin{matrix} s_4 \\ (0.75,0.8,1) \end{matrix} \\ p_2 & (0.3,0.4,0.5) & (0.35,0.65,0.75) & (0.3,0.45,0.5) & (0.4,0.5,0.65) \\ p_3 & (0.6,0.75,0.8) & (0.3,0.5,0.75) & (0.65,0.75,0.75) & (0.3,0.45,0.6) \end{pmatrix}$$

Step 4 : Computing the following relation matrices

$$R_1 = (R_s)_{mem}(\cdot)(R_0)_{mem} = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (0.55,0.7,0.85) \end{matrix} & \begin{matrix} d_2 \\ (0.75,0.8,1) \end{matrix} \\ p_2 & (0.3,0.45,0.55) & (0.4,0.6,0.7) \\ p_3 & (0.6,0.75,0.8) & (0.6,0.7,0.8) \end{pmatrix}$$

$$R_2 = (R_s)_{mem}(\cdot)(J - (R_0)_{mem}) = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (0.7,0.55,0.5) \end{matrix} & \begin{matrix} d_2 \\ (0.65,0.5,0.35) \end{matrix} \\ p_2 & (0.4,0.65,0.5) & (0.35,0.45,0.35) \\ p_3 & (0.5,0.45,0.5) & (0.65,0.5,0.35) \end{pmatrix}$$

$$R_3 = (J - (R_s)_{mem})(\cdot)(R_0)_{mem} = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (0.45,0.3,0.35) \end{matrix} & \begin{matrix} d_2 \\ (0.45,0.5,0.35) \end{matrix} \\ p_2 & (0.7,0.55,0.5) & (0.6,0.55,0.5) \\ p_3 & (0.4,0.45,0.4) & (0.7,0.55,0.4) \end{pmatrix}$$

$$R_4 = \max\{R_2, R_3\} = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (0.7,0.55,0.5) \end{matrix} & \begin{matrix} d_2 \\ (0.65,0.5,0.35) \end{matrix} \\ p_2 & (0.7,0.65,0.5) & (0.6,0.55,0.5) \\ p_3 & (0.5,0.45,0.5) & (0.7,0.55,0.4) \end{pmatrix}$$

$$R_5 = R_1 - R_4 = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (-0.15,0.15,0.35) \end{matrix} & \begin{matrix} d_2 \\ (0.10,0.3,0.65) \end{matrix} \\ p_2 & (-0.4, -0.2,0.05) & (-0.2,0.05,0.2) \\ p_3 & (0.1,0.3,0.3) & (-0.1,0.15,0.4) \end{pmatrix}$$

Step 5 :

$$R_6 = \begin{pmatrix} p_1 & \begin{matrix} d_1 \\ (0.1167) \end{matrix} & \begin{matrix} d_2 \\ (0.35) \end{matrix} & \text{Row}'_i = \text{Max. of the } i \text{ th row} \\ p_2 & (-0.183) & (0.0167) & 0.35 \\ p_3 & (0.233) & (0.15) & 0.0167 \\ & & & 0.233 \end{pmatrix}$$

$p_1$  and  $p_2$  is suffering from dengue and  $p_3$  is suffering from swine flu.

#### IV. DECISION MAKING UNDER FUZZY ENVIROMENT

##### PROCEDURE

Step 1 : Gather the imprecise estimation needed for the problem which is in the form of triangular fuzzy number matrix using equation (1).

Step 2 : Calculate the triangular membership matrix using equation (2).

Step 3 : By using equation (3). Let us calculate all of the relativity values  $f(x_i/x_j)$ , from the comparsion matrix using definition 2.6, this gives the solution to the required problem.

$$\text{Here } f(x_i/x_j) = \frac{(0,0,0)}{(1,1,1)} \text{ for } i = j$$

##### Definition 4.1 : Relativity Function

Let  $x$  and  $y$  be Variables defined on a Universal Set  $X$ . The relativity function is denoted as  $f(x/y)$  and is defined as

$$f(x/y) = \frac{\mu_y(x) - \mu_x(y)}{\max(\mu_y(x), \mu_x(y))} \tag{1}$$

where  $\mu_y(x)$  is the membership function of  $x$  with respect to  $y$  for triangular fuzzy number.

##### Illustrative

##### Example : 4.1

Step 1 : Let us find out who resembles a Grandmother most among her grand elder daughter ( $x_1$ ), her Grand younger daughter ( $x_2$ ) and her Grand son ( $x_3$ ). we have the following imprecise estimations from family members.

Here  $\mu_y(x) - \mu_x(y)$  is calculated using subtraction operation and  $\max(\mu_y(x), \mu_x(y))$  is calculated using definition 2.4.

##### Definition: 4.2 Comparison Matrix

Let  $A = (x_1, x_2, \dots, x_{i-1}, x_i, x_{i+1}, \dots, x_n)$  be a set of  $n$  variables defined on  $X$ . Form a matrix of relativity values  $f(x_i/x_j)$  where  $x_i$ 's for  $i = 1$  to  $n$  are  $n$  variables defined on an universe  $X$ . The matrix  $C = (c_{ij})$  is a square matrix of order  $n$  is called the comparison matrix (or)  $C -$  matrix,

$$\text{with } AM \left( f(x_i/x_j) \right) = \frac{AM(\mu_{x_j}(x_i) - \mu_{x_i}(x_j))}{AM(\max\{\mu_{x_j}(x_i) - \mu_{x_i}(x_j)\})}$$

where  $AM$  denote the Arithmetic mean and it is calculated using definition 2.5. The comparison matrix is used to rank different fuzzy sets, the elements of  $C -$  matrix  $\in [-1,1]$ . The smaller value in the  $i$ th row of the comparison matrix, that is  $C_i = \min\{f(x_i/X), i = 1$  to  $n\}$  variable. The minimum of  $\{C_i'/i = 1$  to  $n\}$ , that is, the smallest value in each of the rows of the  $C -$  matrix will have the lowest weight for ranking purpose. Thus ranking the variable  $x_1, x_2, \dots, x_n$  are determined by ordering the membership values  $C_1', C_2', \dots, C_n'$ .

$$A = \begin{matrix} & \begin{matrix} x_1 & x_2 & x_3 \end{matrix} \\ \begin{matrix} x_1 \\ x_2 \\ x_3 \end{matrix} & \begin{pmatrix} (10,10,10) & (6,7,8) & (2,4,6) \\ (2,4,6) & (10,10,10) & (5,6,7) \\ (2,4,6) & (1,3,5) & (10,10,10) \end{pmatrix} \end{matrix}$$

**Step 2 :** Calculate the triangular membership matrix using equation (2).

$$A_{mem} = \begin{matrix} & \begin{matrix} x_1 & x_2 & x_3 \end{matrix} \\ \begin{matrix} x_1 \\ x_2 \\ x_3 \end{matrix} & \begin{pmatrix} (1,1,1) & (0.6,0.7,0.8) & (0.2,0.4,0.6) \\ (0.2,0.4,0.6) & (1,1,1) & (0.5,0.6,0.7) \\ (0.2,0.4,0.6) & (0.1,0.3,0.5) & (1,1,1) \end{pmatrix} \end{matrix}$$

$$\mu_{x_1}(x_1) = (1,1,1), \quad \mu_{x_2}(x_1) = (0.6,0.7,0.8), \quad \mu_{x_3}(x_1) = (0.2,0.4,0.6),$$

$$\mu_{x_1}(x_2) = (0.2,0.4,0.6), \quad \mu_{x_2}(x_2) = (1,1,1), \quad \mu_{x_3}(x_2) = (0.5,0.6,0.7),$$

$$\mu_{x_1}(x_3) = (0.2,0.4,0.6), \quad \mu_{x_2}(x_3) = (0.1,0.3,0.5), \quad \mu_{x_3}(x_3) = (1,1,1),$$

**Step 3 :**

$$f(x_1/x_1) = \frac{\mu_{x_1}(x_1) - \mu_{x_1}(x_1)}{\max\{\mu_{x_1}(x_1), \mu_{x_1}(x_1)\}} = \frac{\{(1,1,1) - (1,1,1)\}}{\max\{(1,1,1), (1,1,1)\}} = \frac{(0,0,0)}{(1,1,1)}$$

$$AMf(x_1/x_1) = \frac{0}{1} = 0$$

$$f(x_1/x_2) = \frac{\mu_{x_2}(x_1) - \mu_{x_1}(x_2)}{\max\{\mu_{x_2}(x_1), \mu_{x_1}(x_2)\}} = \frac{\{(0.6,0.7,0.8) - (0.2,0.4,0.6)\}}{\max\{(0.6,0.7,0.8), (0.2,0.4,0.6)\}} = \frac{(0,0.3,0.6)}{(0.6,0.7,0.8)}$$

$$AMf(x_1/x_2) = \frac{0.3}{0.7} = 0.428$$

$$f(x_1/x_3) = \frac{\mu_{x_3}(x_1) - \mu_{x_1}(x_3)}{\max\{\mu_{x_3}(x_1), \mu_{x_1}(x_3)\}} = \frac{\{(0.2,0.4,0.6) - (0.2,0.4,0.6)\}}{\max\{(0.2,0.4,0.6), (0.2,0.4,0.6)\}} = \frac{(-0.4,0,0.4)}{(0.2,0.4,0.6)}$$

$$AMf(x_1/x_3) = \frac{0}{0.4} = 0$$

$$f(x_2/x_1) = \frac{\mu_{x_1}(x_2) - \mu_{x_2}(x_1)}{\max\{\mu_{x_1}(x_2), \mu_{x_2}(x_1)\}} = \frac{\{(0.2,0.4,0.6) - (0.6,0.7,0.8)\}}{\max\{(0.2,0.4,0.6), (0.6,0.7,0.8)\}} = \frac{(-0.6, -0.3,0)}{(0.6,0.7,0.8)}$$

$$AMf(x_2/x_1) = \frac{-0.3}{0.7} = -0.43$$

$$f(x_2/x_2) = \frac{\mu_{x_2}(x_2) - \mu_{x_2}(x_2)}{\max\{\mu_{x_2}(x_2), \mu_{x_2}(x_2)\}} = \frac{\{(1,1,1) - (1,1,1)\}}{\max\{(1,1,1), (1,1,1)\}} = \frac{(0,0,0)}{(1,1,1)}$$

$$AMf(x_2/x_2) = \frac{0}{1} = 0$$

$$f(x_2/x_3) = \frac{\mu_{x_3}(x_2) - \mu_{x_2}(x_3)}{\max\{\mu_{x_3}(x_2), \mu_{x_2}(x_3)\}} = \frac{\{(0.5,0.6,0.7) - (0.1,0.3,0.5)\}}{\max\{(0.5,0.6,0.7), (0.1,0.3,0.5)\}} = \frac{(0,0.3,0.6)}{(0.5,0.6,0.7)}$$

$$AMf(x_2/x_3) = \frac{0.3}{0.6} = 0.5$$

$$f(x_3/x_1) = \frac{\mu_{x_1}(x_3) - \mu_{x_3}(x_1)}{\max\{\mu_{x_1}(x_3), \mu_{x_3}(x_1)\}} = \frac{\{(0.2,0.4,0.6) - (0.2,0.4,0.6)\}}{\max\{(0.2,0.4,0.6), (0.2,0.4,0.6)\}} = \frac{0}{(0.2,0.4,0.6)}$$

$$AMf(x_3/x_1) = \frac{0}{0.6} = 0$$

$$f(x_3/x_2) = \frac{\mu_{x_2}(x_3) - \mu_{x_3}(x_2)}{\max\{\mu_{x_2}(x_3), \mu_{x_3}(x_2)\}} = \frac{\{(0.1,0.3,0.5) - (0.5,0.6,0.7)\}}{\max\{(0.1,0.3,0.5), (0.5,0.6,0.7)\}} = \frac{(-0.6, -0.3,0)}{0.5,0.6,0.7}$$

$$AMf(x_3/x_2) = \frac{-0.3}{0.6} = -0.5$$

$$f(x_3/x_3) = \frac{\mu_{x_3}(x_3) - \mu_{x_3}(x_3)}{\max\{\mu_{x_3}(x_3), \mu_{x_3}(x_3)\}} = \frac{\{(1,1,1) - (1,1,1)\}}{\max\{(1,1,1), (1,1,1)\}} = \frac{0}{(1,1,1)}$$

$$AMf(x_3/x_3) = \frac{0}{1} = 0$$

The Comparison matrix  $C = (c_{ij}) = AM(f(x_i/x_j))$  is given by

$$A = \begin{matrix} & \begin{matrix} x_1 & x_2 & x_3 \end{matrix} \\ \begin{matrix} x_1 \\ x_2 \\ x_3 \end{matrix} & \begin{bmatrix} 0 & 0.428 & 0 \\ -0.43 & 0 & 0.5 \\ 0 & -0.5 & 0 \end{bmatrix} \end{matrix} \quad c_i' = \text{min of } i\text{th row}$$

For this problem the ranking is  $x_1, x_2, x_3$ . Hence Grand elder daughter resembles a Grand mother ‘most’

### CONCLUSION

Medicine is one of the field in which the applicability of fuzzy set theory was recognized quite early. As fuzzy decision making is a most important scientific, social and economic endeavour, there exist several major approaches within the theories of fuzzy decision making. Here we have used the ranking order to deal with the vagueness in imprecise determination of preferences.

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